
Einladung zu einem Vortrag
im Rahmen des DK-Seminars des Karl Popper Kollegs von

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zum Thema

**Hilbert's Nullstellensatz and Linear Algebra:
An Algorithm for Determining Combinatorial
Infeasibility**

Ort: I.2.01 der Universität Klagenfurt

Zeit: Mittwoch, 08. März 2017, um 10 Uhr c.t.

Kurzfassung:

Unlike systems of linear equations, systems of multivariate polynomial equations over the complex numbers or finite fields can be compactly used to model combinatorial problems. In this way, a problem is feasible (e.g. a graph is 3-colorable, Hamiltonian, etc.) if and only if a given system of polynomial equations has a solution. Via Hilbert's Nullstellensatz, we generate a sequence of large-scale, sparse linear algebra computations from these non-linear models to describe an algorithm for solving the underlying combinatorial problem. As a byproduct of this algorithm, we produce algebraic certificates of the non-existence of a solution (i.e., non-3-colorability, non-Hamiltonicity, or non-existence of an independent set of size k).

In this talk, we present theoretical and experimental results on the size of these sequences, and the complexity of the Hilbert's Nullstellensatz algebraic certificates. For non-3-colorability over a finite field, we utilize this method to successfully solve graph problem instances having thousands of nodes and tens of thousands of edges. We also describe methods of optimizing this method, such as finding alternative forms of the Nullstellensatz, adding carefully-constructed polynomials to the system, branching and exploiting symmetry.

Das Institut für Mathematik freut sich auf Ihren Besuch.

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